

Chapter 1: Review

Section 1: Functions

page 15: 1, 3, 5, 7, 19, 25

Section 2: Operations on Functions

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Section 3: Linear Functions

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Section 4: Exponents

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1.1

Memorize one of these or the equivalent.

**Function**

**Function:** A rule for a relationship between an input, or independent, quantity and an output, or dependent, quantity in which each input value uniquely determines one output value. We say “the output is a function of the input.”

Definition: A function is a rule that associates to each element of one set, called the domain, a unique corresponding element in another set (which could be identical to the original set), called the range.

Memorize

**Function Notation**

The notation  $\text{output} = f(\text{input})$  defines a function named  $f$ .  
This would be read “output is  $f$  of input”

Example

$$f(x) = x^2, \quad x \in \mathbb{R}$$

$x$  is an element, or member,  
of the set all real numbers

1.3

Memorize

**Laws of Exponents:**

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All variables here represent real numbers and all variables in denominators are nonzero.

$$1) x^a \cdot x^b = x^{a+b}$$

$$2) \frac{x^a}{x^b} = x^{a-b}$$

$$3) (x^a)^b = x^{ab}$$

$$4) (xy)^a = x^a y^a$$

$$5) \left(\frac{x}{y}\right)^b = \frac{x^b}{y^b}$$

$$6) x^0 = 1, \text{ provided } x \neq 0$$

$$7) x^{-n} = \frac{1}{x^n}, \text{ provided } x \neq 0$$

$$8) x^{1/n} = \sqrt[n]{x}, \text{ provided } x \neq 0$$

$$2^3 \cdot 2^2 = (2 \times 2 \times 2) (2 \times 2)$$

$$\Rightarrow 2 \times 2 \times 2 \times 2 \times 2$$

$$= 2^5$$

$$= 2^{3+2}$$

$$\frac{2^5}{2^2} = \frac{\cancel{2} \cdot \cancel{2} \cdot 2 \cdot 2 \cdot 2}{\cancel{2} \cdot \cancel{2}}$$

$$= 2^3 = 2^{5-2}$$

$$(2^3)^2 = (2^3)(2^3)$$

$$= 2^{3+3} = 2^6 = 2^{(3)(2)}$$

$$\frac{2^3}{2^3} = \frac{8}{8} = 1$$

$$1 \quad 1 \quad 2 \quad - \quad 3-3 \quad - \quad 0$$

$$\text{by rule } \frac{2^2}{2^3} = 2^{2-3} = 2^{-1}$$

To keep our beautiful rule

define  $2^0 = 1$

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$$\frac{2^2}{2^4} = \frac{\cancel{2} \cdot \cancel{2}}{\cancel{2} \cdot \cancel{2} \cdot 2 \cdot 2} = \frac{1}{2^2}$$

rule:  $\frac{2^2}{2^4} = 2^{2-4} = 2^{-2}$

define  $2^{-2} = \frac{1}{2^2}$

$$\boxed{b^{-n} = \frac{1}{b^n}}$$


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$$\frac{2^3}{2^2} = \frac{8}{4} = 2$$

by rule  $\frac{2^3}{2^2} = 2^{3-2} = 2^1$

Define  $2^1 = 2$

$$\boxed{b^1 = b}$$

1 1 1 + 1 1 1

$$\overbrace{b^{\frac{1}{2}} \cdot b^{\frac{1}{2}}} = b^{\frac{1}{2} + \frac{1}{2}} = b^1 = b$$

$$\sqrt{b} \sqrt{b} = b$$

$$\text{define } b^{\frac{1}{2}} = \sqrt{b}$$