11-11-25 MTH 167-004N

7.3 Parabolas

7.3.1 Exercises

page 512 (524): 1, 4, 11, 19

7.4 Ellipses

7.4.1 Exercises

page 525 (537): 2, 6, 9, 16

7.5 Hyperbolas

7.5.1 Exercises

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10 Foundations of Trigonometry

10.1 Angles and their Measure

10.1.2 Exercises

page 709 (721): 9, 15, 17, 30, 35, 39, 41, 50

Math Club: Our club is open to all students, regardless of their current math level. We provide a fun and engaging space to explore math topics, connect with peers, and learn about new opportunities. We meet biweekly on Mondays from 3:00 PM to 4:00 PM in CT-121 (MDE Lab).



2nd Annual Integration Bee: This is a fun and challenging competition with over \$300 in prizes. It's a great event for students to test their calculus skills and even challenge their professors! We'll have snacks, and all are welcome to attend, even just to watch.

- Date: Friday, November 21st
- Time: 3:00 PM
- Location: CA 302 (Annandale Campus)
- Calculus II experience is recommended for competitors.



Putnam Mathematical Competition: We are actively recruiting and training students for the Putnam, the nation's top collegiate math competition. This is a fantastic opportunity for students seeking a serious challenge.

- Exam Date: Saturday, December 6th
- Training Sessions: Mondays from 4:00 PM to 5:00 PM in CT-121
- Open to all, though experience in Calculus III and Linear Algebra is recommended.



We would be very grateful if you could forward this email, along with the attached flyers, to the Annandale math faculty. Their support is invaluable for getting students involved.

Thank you for your time and for supporting student engagement in mathematics.

Emiliano Mercado NVCCMathClubAN@gmail.com

7.3: 19

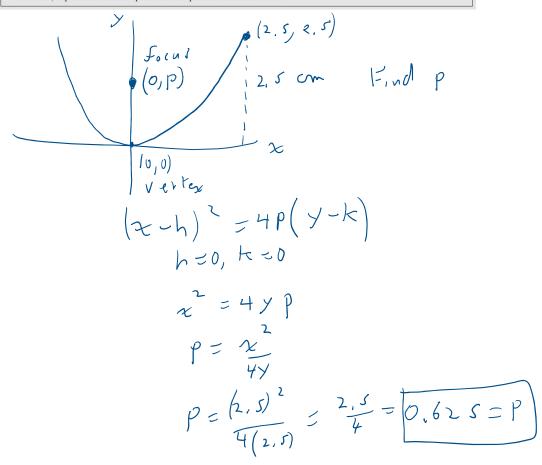
19. The mirror in Carl's flashlight is a paraboloid of revolution. If the mirror is 5 centimeters in diameter and 2.5 centimeters deep, where should the light bulb be placed so it is at the focus of the mirror?

Equation 7.2. The Standard Equation of a Vertical^a Parabola: The equation of a (vertical) parabola with vertex (h, k) and focal length |p| is

$$(x-h)^2 = 4p(y-k)$$

If p > 0, the parabola opens upwards; if p < 0, it opens downwards.

^aThat is, a parabola which opens either upwards or downwards.

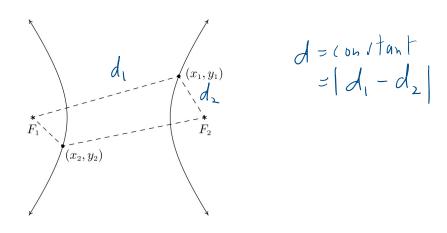


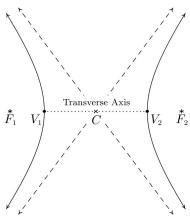
The bulb should be placed 2.5 cm above the base of the mirror, i.e. the focus is 2.5 cm above the vertex.

7.5

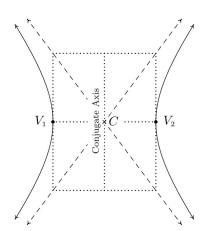
Supplied locus definition

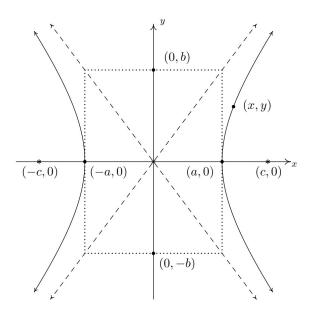
Definition 7.6. Given two distinct points F_1 and F_2 in the plane and a fixed distance d, a **hyperbola** is the set of all points (x, y) in the plane such that the absolute value of the difference of each of the distances from F_1 and F_2 to (x, y) is d. The points F_1 and F_2 are called the **foci** of the hyperbola.





A hyperbola with center C; foci $F_1,\,F_2;$ and vertices $V_1,\,V_2$ and asymptotes (dashed)





Supplied

Equation 7.6. The Standard Equation of a Horizontal Hyperbola For positive numbers a and b, the equation of a horizontal hyperbola with center (h, k) is

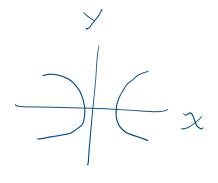
$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$



^aThat is, a hyperbola whose branches open to the left and right

Equation 7.7. The Standard Equation of a Vertical Hyperbola For positive numbers a and b, the equation of a vertical hyperbola with center (h,k) is:

$$\frac{(y-k)^2}{b^2} - \frac{(x-h)^2}{a^2} = 1$$

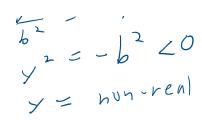


$$\frac{\chi^{2} - y^{2}}{\delta^{2}} = 1$$

$$\frac{\chi^{2}}{\delta^{2}} = 1 + \frac{y^{2}}{\delta^{2}}$$

$$\frac{\chi^{2}}{\delta^{2}} = 1 + \frac{y^{2}}{\delta^{2}}$$

$$\chi^{2} = 1 + \frac{$$



Supplied

Strategies for Identifying Conic Sections

Suppose the graph of equation $Ax^2 + Cy^2 + Dx + Ey + F = 0$ is a non-degenerate conic section.

• If just one variable is squared, the graph is a parabola. Put the equation in the form of Equation 7.2 (if x is squared) or Equation 7.3 (if y is squared).

If both variables are squared, look at the coefficients of x^2 and y^2 , A and B.

- If $A = \mathbb{R}$ the graph is a circle. Put the equation in the form of Equation 7.1.
- If $A \neq R$ but A and R have the *same sign*, the graph is an ellipse. Put the equation in the form of Equation 7.4.
- If A and R have the different signs, the graph is a hyperbola. Put the equation in the form of either Equation 7.6 or Equation 7.7.

^aThat is, a parabola, circle, ellipse, or hyperbola – see Section 7.1.

There is a more general equation

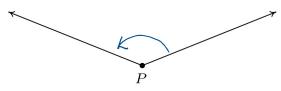
 $Ax^{2} + Bxy + Cy^{2} + Dx + Ey + F = 0$ the conic

(ection

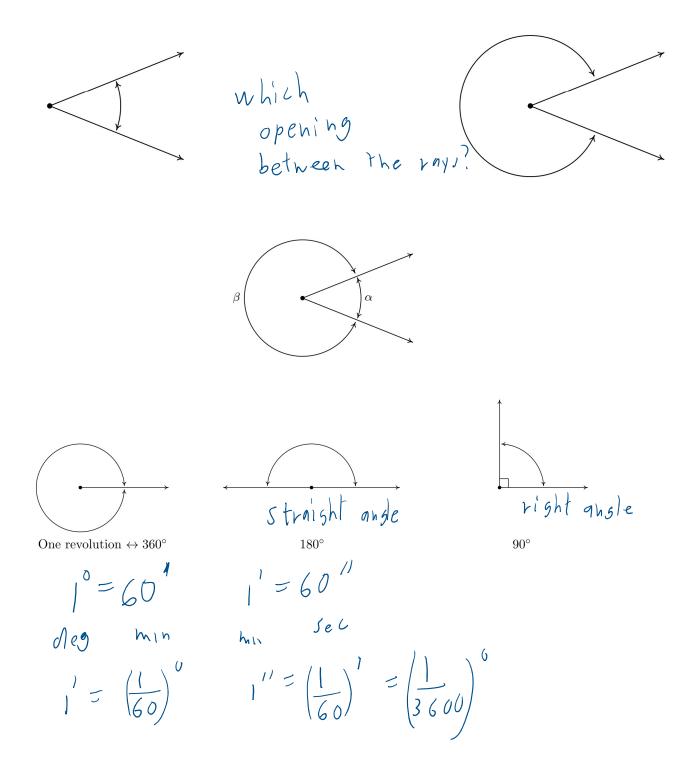
10.1 Memorize



A ray with initial point P.

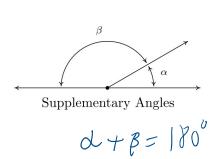


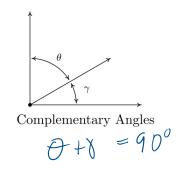
An angle with vertex P.



DD = decimal degree
DMS = degree-minute-second

Memorize





Memorize

Definition 10.1. The real number π is defined to be the ratio of a circle's circumference to its diameter. In symbols, given a circle of circumference C and diameter d,

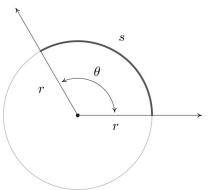
$$\pi = \frac{C}{d}$$

$$d = diometer = (2)(radius) = 2r$$

$$(7) = \frac{C}{2r}$$

$$(C = 2 + 1)$$

Memorize



se arc length
revoding

Decentral angle

The radian measure of θ is $\frac{s}{r}$.

S=ro (O in radials)

T = 180°

Tradian = 180°

memorize

$$2\pi = 360^{\circ}$$

$$S = V\theta$$

$$V = C = 2\pi V = V\theta$$

$$\Rightarrow 0 = 2\pi V = 360^{\circ}$$

$$\Rightarrow \pi = 180^{\circ}$$

memorize

Equation 10.2. Velocity for Circular Motion: For an object moving on a circular path of radius r with constant angular velocity ω , the (linear) velocity of the object is given by $v = r\omega$.

$$V = \frac{\Delta S}{\Delta t} = \frac{r \times \phi}{\Delta t} = r \left(\frac{\Delta \phi}{\Delta t}\right)$$

$$= r w \text{ angle time}$$

$$= r w \text{ angle time}$$

$$= r \text{ angle time}$$

7.5

In Exercises 1 - 8, graph the hyperbola. Find the center, the lines which contain the transverse and conjugate axes, the vertices, the foci and the equations of the asymptotes.

2.
$$\frac{y^2}{9} - \frac{x^2}{16} = 1$$

Equation 7.7. The Standard Equation of a Vertical Hyperbola For positive numbers a and b, the equation of a vertical hyperbola with center (h, k) is:

$$\frac{(y-k)^2}{b^2} - \frac{(x-h)^2}{a^2} = 1$$

center =
$$(h, k) = (0, 0)$$
 $a^2 = 16 \Rightarrow (a = 4)$

$$a^{2} = 16 \Rightarrow a = 4$$

$$b^{2} = 9 \Rightarrow b^{2} = 3$$

$$(0,3) \times fo(n) (0,2)$$

$$(0,4) \times fo(n) \times (0,2)$$

$$(0,4) \times f$$

(0,-4) VENTER (0,0) 50(4) (0,-2) = (0,-5)

$$C = \int 0^{1} + b^{2}$$
 $C = \int 4^{2} + 3^{2} = \int 16 + 9 = \int 25 = 5$
 $C = 5$

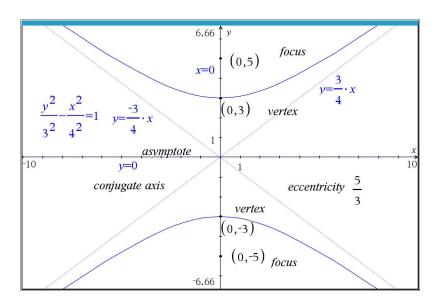
2.
$$\frac{y^2}{9} - \frac{x^2}{16} = 1$$
a $5 \neq \text{imptote}/$

$$\frac{y^2}{9} = 1 + \frac{x^2}{16}$$

$$y^2 = 1 + \frac{x^2}{16}$$

$$y^2 = 1 + \frac{x^2}{16}$$

$$y = \pm 3 \frac{x^2}{16}$$
Ary imptote
$$y \rightarrow \pm 3 \frac{x^2}{16}$$
Ary imptote
$$y \rightarrow \pm 3 \frac{x^2}{16}$$



supplied

 $e = \frac{\text{distance from the center to a focus}}{\text{distance from the center to a vertex}}$

Copilot

supplied

I'm in my precalculus class. Could you tell me how eccentricity can distinguish between different types of conic sections?

Eccentricity classifies conic sections based on their shapes. For circles, the eccentricity is zero. Ellipses have an eccentricity between zero and one. Parabolas have an eccentricity of exactly one, and hyperbolas have an eccentricity greater than one. This value indicates how "stretched" the conic section is.