

## General introduction

14 class meetings before final exam

30 textbook sections and extra topics

$$30/14=2.1429$$

Two or three sections per class meeting

## 1. Operations with Real Numbers

## 1.1 Algebraic Expressions

1.1 Exercise Set, page 40 (22): 1, 3, 5, 7, 9, 10, 12, 22, 27

Your Name MTH 111 bonus quiz 1

Write each problem. Put a box around each answer.

1. Add 35.4 and 41.6

$$\begin{array}{r} 35.4 \\ 41.6 \\ \hline 77.0 \end{array}$$

$$\boxed{77.0}$$

No calculator.

2. Find the difference between 183 and 75

$$\begin{array}{r} 183 \\ - 75 \\ \hline 108 \end{array}$$

$$\boxed{108}$$

3. 1 foot = 12 inches

$$\Rightarrow \frac{1 \text{ ft}}{12 \text{ in}} = 1 = \frac{12 \text{ in}}{1 \text{ ft}}$$

5280 feet = 1 mile

How many inches are there in 1 mile?

$$\frac{5280 \text{ ft}}{1 \text{ mile}} = 1 = \frac{1 \text{ mi}}{5280 \text{ ft}}$$

$$1 \text{ mile} = (1 \text{ mile})(1) = (1 \text{ mile}) \left( \frac{5280 \text{ ft}}{1 \text{ mi}} \right) \left( \frac{12 \text{ in}}{1 \text{ ft}} \right)$$

$$\begin{array}{r} 5280 \\ \times 12 \\ \hline 10560 \\ 5280 \\ \hline 63360 \end{array}$$

$$= \boxed{63,360 \text{ in.}}$$

$$5280 \cdot 12 = 63360$$

4. Solve and show your check  $2x - 5 = 11$ 

$$\text{check } 2x = 16 \quad \left| \begin{array}{l} \text{long, detailed, complete} \\ \text{ } \end{array} \right. \quad \begin{array}{l} 2x - 5 = 11 \\ 2(8) - 5 = 11 \\ 16 - 5 = 11 \\ 11 = 11 \end{array}$$

4. Solve and show your check  $2x - 5 = 11$

Good  
elegant

$$2x = 16$$

$$x = 8$$

long, detailed, complete

$$2x - 5 = 11$$

$$2x - 5 + 5 = 11 + 5$$

$$2x + (-5 + 5) = 16$$

$$2x + 0 = 16$$

$$2x = 16$$

$$2x = \frac{16}{2}$$

$$1)x = 8$$

$$x = 8$$

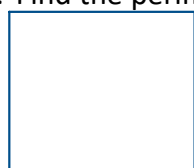
check

$$2(8) - 5 = 11$$

$$16 - 5 = 11$$

$$11 = 11 \checkmark$$

5. Find the perimeter and area of the square with side = 3 cm



3 cm

$$\text{Perimeter} = 3 \text{ cm} + 3 \text{ cm} + 3 \text{ cm} + 3 \text{ cm}$$

$$\text{area} = (3 \text{ cm})^2 = 3^2 \text{ cm}^2 = 9 \text{ cm}^2$$

$$= 4(3 \text{ cm}) = 12 \text{ cm}$$

6. Add and simplify  $\frac{2}{3} + \frac{1}{5}$

$$\frac{2}{3} \left( \frac{5}{5} \right) + \left( \frac{1}{5} \right) \left( \frac{3}{3} \right) = \frac{10}{15} + \frac{3}{15}$$

$$= \frac{10+3}{15} = \frac{13}{15}$$

7. Write as a single number  $\frac{4 \times 1000}{2 \times 100}$

$$= (2) \left( \frac{1000}{100} \right) = (2)(10) = 20$$

$$\frac{4 \times 10^3}{2 \times 10^2} = 2 \times 10^{3-2} = 2 \times 10^1 = 20$$

scientific  
notation

8. What is 15% of 80?

$$x = 15 \left( \frac{1}{100} \right) (80)$$

$$x = (15) \left( \frac{8}{10} \right)$$

$$= (5.3) (8)$$

$$\% = \frac{1}{100} = 0.01$$

$$0.15 \times 80 = 12.0$$

$$= \frac{(5 \cdot 3)(8)}{5 \cdot 2}$$

$$0.15 \cdot 80 = 12.0$$

$$x = 12$$

12 is 15% of 80

## 1.1

### Memorize

#### Variables and Constants

A variable is a letter that represents a number or quantity whose value may change.

A constant is a number whose value always stays the same.

### Memorize

Operation	Notation	Say:	The result is...
Addition	$a + b$	$a$ plus $b$	the sum of $a$ and $b$
Subtraction	$a - b$	$a$ minus $b$	the difference of $a$ and $b$
Multiplication	$a \cdot b$ , $(a)(b)$ , $(a)b$ , $a(b)$	$a$ times $b$	The product of $a$ and $b$
Division	$a \div b$ , $a/b$ , $\frac{a}{b}$ , $b \overline{)a}$	$a$ divided by $b$	The quotient of $a$ and $b$

### Memorize

Algebraic Notation	Say
$a = b$	$a$ is equal to $b$
$a \neq b$	$a$ is not equal to $b$
$a < b$	$a$ is less than $b$
$a > b$	$a$ is greater than $b$
$a \leq b$	$a$ is less than or equal to $b$
$a \geq b$	$a$ is greater than or equal to $b$

### Memorize

## Common Grouping Symbols

Name	Symbol
parentheses	( )
brackets	[ ]
braces	{ }

Memorize

### Expressions and Equations

An expression is a number, a variable, or a combination of numbers and variables and operation symbols.  
An equation is made up of two expressions connected by an equal sign.

Memorize

### Exponential Notation (Power)

For any expression  $a^n$ ,  $a$  is a factor multiplied by itself  $n$  times if  $n$  is a positive integer.  
 $a^n$  means multiply  $n$  factors of  $a$

The diagram illustrates the components of exponential notation. At the top, the word "base" in red is followed by a right-pointing arrow to the letter  $a$  in  $a^n$ . A left-pointing arrow from the word "exponent" in blue points to the superscript  $n$ . Below this, the equation  $a^n = a \cdot a \cdot a \cdot \dots \cdot a$  is shown. A blue bracket underneath the series of  $a$ 's is labeled " $n$  factors" in blue.

The expression  $a^n$  is read  $a$  to the  $n^{th}$  power.

Memorize

## Order of Operations

When simplifying mathematical expressions perform the operations in the following order:

### 1. Parentheses and other Grouping Symbols

- Simplify all expressions inside the parentheses or other grouping symbols, working on the innermost parentheses first.

### 2. Exponents

- Simplify all expressions with exponents.

### 3. Multiplication and Division

- Perform all multiplication and division in order from left to right. These operations have equal priority.

### 4. Addition and Subtraction

- Perform all addition and subtraction in order from left to right. These operations have equal priority.

Students often ask, "How will I remember the order?" Here is a way to help you remember: Take the first letter of each key word and substitute the silly phrase.

**Please Excuse My Dear Aunt Sally.**

Laws of exponents.

$$2^3 \cdot 2^2 = (8)(4) = 32$$

$$= (2, 2, 2)(2, 2)$$

$$= 2, 2, 2, 2, 2$$

$$= 2^5 = 2^{3+2}$$

$$a^m \cdot a^n = a^{m+n}$$

$$\boxed{\frac{a^m}{a^n} = a^{m-n}}$$

$$\frac{a^m}{a^m} = 1$$

by rule  $\frac{a^m}{a^m} = a^{m-m} = a^0$

To keep our beautiful rule  
define  $a^0 = 1$

$$\frac{2^3}{2^5} = \frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{2}^1}{\cancel{2} \cdot \cancel{2} \cdot \cancel{2} \cdot 2 \cdot 2} = \frac{1}{2^2}$$

rule  $\frac{2^3}{2^5} = 2^{3-5} = 2^{-2}$   
define  $2^{-2} = \frac{1}{2^2}$

$$\boxed{a^{-n} = \frac{1}{a^n}}$$

$$a^{\frac{1}{2}} \cdot a^{\frac{1}{2}} = a^{\frac{1}{2} + \frac{1}{2}} = a^1 = a$$

$$\sqrt{a} \sqrt{a} = a$$

define  $\boxed{a^{\frac{1}{2}} = \sqrt{a}}$