

General introduction

14 class meetings before final exam

30 textbook sections and extra topics

30/14=2.1429

Two or three sections per class meeting

1. Operations with Real Numbers

1.1 Algebraic Expressions

1.1 Exercise Set, page 40 (22): 1, 3, 5, 7, 9, 10, 12, 22, 27

Your Name MTH 111 bonus quiz 1

1. Add 35.4 and 41.6

$$\begin{array}{r}
 35.4 \\
 +41.6 \\
 \hline
 77.0
 \end{array}$$

Write each problem. Put a box around each answer.

No calculator.

$$\boxed{77.0}$$

2. Find the difference between 183 and 75

$$\begin{array}{r}
 183 \\
 -75 \\
 \hline
 108
 \end{array}$$

$$\boxed{108}$$

3. 1 foot = 12 inches $\Rightarrow \frac{1 \text{ ft}}{12 \text{ in}} = 1 = \frac{12 \text{ in}}{1 \text{ ft}}$
5280 feet = 1 mile

How many inches are there in 1 mile?

$$\frac{5280 \text{ ft}}{1 \text{ mile}} = 1 = \frac{1 \text{ mi}}{5280 \text{ ft}}$$

$$\begin{aligned}
 1 \text{ mile} &= (1 \text{ mile})(1) = (1 \text{ mile}) \left(\frac{5280 \text{ ft}}{1 \text{ mi}} \right) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right) \\
 &= \boxed{63,360 \text{ in}}
 \end{aligned}$$

$$5280 \times 12 = 63360$$

4. Solve and show your check $2x - 5 = 11$

$$\begin{array}{r}
 2x = 16 \\
 \hline
 \end{array}
 \quad \mid \text{long, detailed, complete}$$

4. Solve and show your check $2x - 5 = 11$

Good elegant $2x = 16$ long, detailed, complete

$x = 8$

$$\begin{aligned}
 2x - 5 &= 11 \\
 2x - 5 + 5 &= 11 + 5 \\
 2x + (-5+5) &= 16 \\
 2x + 0 &= 16 \\
 2x &= 16 \\
 \frac{2x}{2} &= \frac{16}{2} \\
 11(x) &= 8 \\
 x &= 8
 \end{aligned}$$

check

$$\begin{aligned}
 2(8) - 5 &= 11 \\
 16 - 5 &= 11 \\
 11 &= 11 \quad \checkmark
 \end{aligned}$$

5. Find the perimeter and area of the square with side = 3 cm

 3 cm

$$\begin{aligned}
 \text{Perimeter} &= 3 \text{ cm} + 3 \text{ cm} \\
 &\quad + 3 \text{ cm} + 3 \text{ cm} \\
 \text{area} &= (3 \text{ cm})^2 = 9 \text{ cm}^2 \\
 &= 4(3 \text{ cm}) = 12 \text{ cm}
 \end{aligned}$$

6. Add and simplify $\frac{2}{3} + \frac{1}{5}$

$$\begin{aligned}
 \frac{2}{3} \left(\frac{5}{5} \right) + \left(\frac{1}{5} \right) \left(\frac{3}{3} \right) &= \frac{10}{15} + \frac{3}{15} \\
 &= \frac{10+3}{15} = \frac{13}{15}
 \end{aligned}$$

7. Write as a single number $\frac{4 \times 1000}{2 \times 100}$

$$\begin{aligned}
 &= (2) \left(\frac{1000}{100} \right) = (2)(10) = 20 \\
 \frac{4 \times 10^3}{2 \times 10^2} &= 2 \times 10^{3-2} = 2 \times 10^1 = 20
 \end{aligned}$$

scientific notation

8. What is 15% of 80?

$$\begin{aligned}
 x &= 15 \left(\frac{1}{100} \right) \cdot (80) \\
 x &= (15) \left(\frac{8}{10} \right) \\
 &= \cancel{(5 \cdot 3)} \cancel{(8)} \quad 0.15 \cdot 80 = 12.0
 \end{aligned}$$

$\frac{\%}{100} = \frac{1}{100} = 0.01$

$$= \frac{(x \cdot 3)(x)}{x \cdot x}$$

0.10 00-12.0

$$x = 12$$

12 is 15% of 80

1.1

Memorize

Variables and Constants

A variable is a letter that represents a number or quantity whose value may change.

A constant is a number whose value always stays the same.

Memorize

Operation	Notation	Say:	The result is...
Addition	$a + b$	a plus b	the sum of a and b
Subtraction	$a - b$	a minus b	the difference of a and b
Multiplication	$a \cdot b, (a)(b), (a)b, a(b)$	a times b	The product of a and b
Division	$a \div b, a/b, \frac{a}{b}, b\overline{)a}$	a divided by b	The quotient of a and b

Memorize

Algebraic Notation	Say
$a = b$	a is equal to b
$a \neq b$	a is not equal to b
$a < b$	a is less than b
$a > b$	a is greater than b
$a \leq b$	a is less than or equal to b
$a \geq b$	a is greater than or equal to b

Memorize

Common Grouping Symbols

Name	Symbol
parentheses	()
brackets	[]
braces	{ }

Memorize

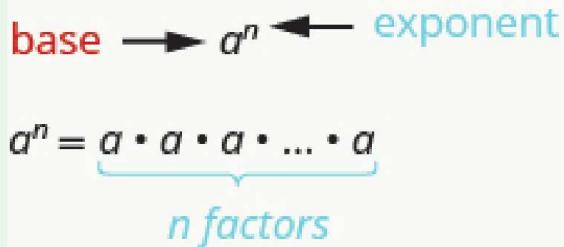
Expressions and Equations

An expression is a number, a variable, or a combination of numbers and variables and operation symbols.
An equation is made up of two expressions connected by an equal sign.

Memorize

Exponential Notation (Power)

For any expression a^n , a is a factor multiplied by itself n times if n is a positive integer.
 a^n means multiply n factors of a



The expression a^n is read a to the n^{th} power.

Memorize

When simplifying mathematical expressions perform the operations in the following order:

1. **Parentheses and other Grouping Symbols**

- Simplify all expressions inside the parentheses or other grouping symbols, working on the innermost parentheses first.

2. **Exponents**

- Simplify all expressions with exponents.

3. **Multiplication and Division**

- Perform all multiplication and division in order from left to right. These operations have equal priority.

4. **Addition and Subtraction**

- Perform all addition and subtraction in order from left to right. These operations have equal priority.

Students often ask, "How will I remember the order?" Here is a way to help you remember: Take the first letter of each key word and substitute the silly phrase.

Please Excuse My Dear Aunt Sally.

Laws of exponents.

$$2^3 \cdot 2^2 = (3)(4) = \boxed{32}$$

$$= (2 \cdot 2 \cdot 2)(2 \cdot 2)$$

$$\begin{aligned} &= 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \\ &= 2^5 = 2^{3+2} \end{aligned}$$

$$a^m \cdot a^n = a^{m+n}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$\frac{a^m}{a^m} = 1$$

by rule $\frac{a^m}{a^m} = a^{m-m} = a^0$

To keep our beautiful rule

define $a^0 = 1$

$$\frac{2^3}{2^5} = \frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{2}^1}{\cancel{2} \cdot \cancel{2} \cdot \cancel{2} \cdot 2 \cdot 2} = \frac{1}{2^2}$$

rule $\frac{2^3}{2^5} = 2^{3-5} = 2^{-2}$

define $2^{-2} = \frac{1}{2^2}$

$$a^{-n} = \frac{1}{a^n}$$

$$a^{\frac{1}{2}} \cdot a^{\frac{1}{2}} = a^{\frac{1}{2} + \frac{1}{2}} = a^1 = a$$

$$\sqrt{a} \sqrt{a} = a$$

define $a^{\frac{1}{2}} = \sqrt{a}$