

Chapter 5 - Ratio, Proportion, and Percent

5.1 Ratio and Proportion

5.1 Exercise Set, page 331: 1, 3, 7, 11, 19, 25, 31, 41, 43, 49, 51, 67

5.2 Introduction to Percent

5.2 Exercise Set, page 342: 1, 3, 5, 9, 13, 31, 37, 45, 53

5.3 Percents and Fractions

5.3 Exercise Set, page 348: 1, 5, 7, 17, 21, 29, 59

5.4 Solving Percent Problems Using Equations

5.4 Exercise Set, page 357: 1, 5, 9, 19, 27, 67

5.5 Solving Percent Problems Using Proportions

5.5 Exercise Set, page 365: 1, 5, 9, 15, 57, 65

5.1: 49

Objective D For each proportion, find the unknown number n . See Examples 11 through 13.

49. $\frac{n}{5} = \frac{6}{10}$

$\frac{n}{5} = \frac{3}{5}$
clearly, $n=3$
 $\left(\frac{n}{\cancel{5}}\right)\left(\cancel{5}\right) = \left(\frac{3}{\cancel{5}}\right)\cancel{5}$
 $n=3$

cross multiply
 $5n = (3)(5)$
 $\cancel{5}n = (3)(\cancel{5})$
 $n=3$

 $10n = (6)(5)$
 $n = \frac{30}{10}$
 $n=3$

Write each percent as a decimal. See Examples 3 through 7.

29. A $\frac{1}{2}$ -cup serving of dried tart cherries delivers 45% of an adult's Daily Value of vitamin A. (Source: USDA Nutrient Data Laboratory)

write 45% as a decimal

$$45\% = 45(0.01)$$

$$= 0.45$$

$$45\% = 45\left(\frac{1}{100}\right) = \frac{45}{100} = 0.45$$

5.3

Examples

Write each fraction or mixed number as a percent.

6. $\frac{9}{20} = \frac{9}{20} \cdot 100\% = \frac{9}{20} \cdot \frac{100}{1}\% = \frac{900}{20}\% = 45\%$

7. $\frac{2}{3} = \frac{2}{3} \cdot 100\% = \frac{2}{3} \cdot \frac{100}{1}\% = \frac{200}{3}\% = 66\frac{2}{3}\%$

8. $1\frac{1}{2} = \frac{3}{2} \cdot 100\% = \frac{3}{2} \cdot \frac{100}{1}\% = \frac{300}{2}\% = 150\%$

Helpful Hint

$$\frac{200}{3} = 66.\bar{6}$$

Thus, another way to write $\frac{200}{3}\%$ is $66.\bar{6}\%$.

$$\frac{9}{20} = \left(\frac{9}{20}\right)\left(\frac{5}{5}\right) = \frac{45}{100} = 45\%$$

$$\frac{102}{51} = 2$$

$$\frac{(36)(36)}{50} = x$$

$$\frac{(18)(2)(18)(2)}{(25)\cancel{x}} = x$$

$$\frac{(324)(2)}{25} = x$$

$$\frac{648}{25} = x$$

$$x = 25 \frac{13}{25}$$

$$\frac{18^2}{324}$$

$$25 \overline{)648} \\ \underline{50} \\ 148 \\ \underline{125} \\ 23$$

5.5

Percent Proportion

$$\frac{\text{amount}}{\text{base}} = \frac{\text{percent}}{100} \quad \leftarrow \text{always 100}$$

or

$$\begin{array}{l} \text{amount} \rightarrow a \\ \text{base} \rightarrow b \end{array} \rightarrow \frac{a}{b} = \frac{p}{100} \quad \leftarrow \text{percent}$$

Example 7 Solving Percent Proportions for the Amount



What number is 30% of 9?

Solution:

amount

percent

base

$$\frac{a}{9} = \frac{30}{100}$$

$$\frac{a}{9} = \frac{30}{100}$$

$$a = (30\%)(9)$$

$$a = (30)\left(\frac{1}{100}\right)(9)$$

$$\frac{a}{9} = \frac{30}{100}$$

Your Name MDE 10 bonus quiz 2 Write each problem.

1. Convert $\frac{3}{8}$ to a percent.

$$\begin{aligned}\frac{3}{8} &= .375 \\ &= .375(100\%) \\ &= \boxed{37.5\%}\end{aligned}$$

$$\begin{array}{r} 375 \\ 8 \overline{) 3.000} \\ \underline{24} \\ 60 \\ \underline{56} \\ 40 \end{array}$$

2. Convert 0.546 to a fraction. Then, reduce the fraction.

$$\frac{546}{1000} = \boxed{\frac{273}{500}}$$

$$\begin{array}{r} 273 \\ 2 \overline{) 546} \\ \underline{4} \\ 14 \\ \underline{14} \\ 60 \\ \underline{60} \\ 0 \end{array}$$

3. 20 is what percent of 10?

$$20 = x\%(10)$$

$$20 = x\left(\frac{1}{100}\right)(10)$$

$$20 = \frac{x}{10}$$

$$x = (20)(10)$$

$$\boxed{x = 200}$$

Therefore, 20 is 200% of 10

x

Therefore, 20 is 200% of 10

2. Solve the proportion $\frac{5}{9} = \frac{n}{45}$.

$$9n = (5)(45)$$

$$n = \frac{(5)(45)}{9} = \frac{(5)(\cancel{9})(5)}{\cancel{9}}$$

$$n = 25$$